

## Solving Pdes Using Laplace Transforms Chapter 15

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Solve PDE via Laplace transforms ~~Laplace Transforms for Partial Differential Equations (PDEs) Solving PDE using Laplace Transform Method (PART 1) ME565 Lecture 25: Laplace transform solutions to PDEs Mod-03 Lec-26 Applications of Laplace Transform to PDEs Lecture 44: Solution of Partial Differential Equations using Laplace Transform Laplace Transform to Solve a Differential Equation, Ex 1, Part 1/2 solve differential with laplace transform, sect 7.5#3 Using Laplace Transforms to Solve Differential Equations How to solve PDE: Laplace transforms Applications of Laplace Transform to PDEs Laplace transform to solve an equation | Laplace transform | Differential Equations | Khan Academy~~

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How to apply Fourier transforms to solve differential equations

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Intro to Fourier transforms: how to calculate them The Laplace Transform: A Generalized Fourier Transform (1:2) Where the Laplace Transform comes from (Arthur Mattuck, MIT) What does the Laplace Transform really tell us? A visual explanation (plus applications) Intro to the Laplace Transform \u0026 Three Examples Fourier Series: Part 1 Exponential Growth is a Lie Laplace transforms vs separation of variables Partial Fractions and Laplace Inverse | MIT 18.03SC Differential Equations, Fall 2011 ~~APPLICATIONS OF LAPLACE TRANSFORMS TO SOLUTIONS OF PARTIAL DIFFERENTIAL EQUATIONS~~ Laplace Transform | Application to Partial Differential Equations | GP Solving Differential Equations Using Laplace Transforms Ex. 1 Laplace Transform Initial Value Problem Example Lecture 45: Solution of Heat Equation and Wave Equation using Laplace Transform Using Laplace Transforms to solve Differential Equations \*\*\*full example\*\*\* ~~Laplace Transforms and Differential Equations~~ Laplace Transform Examples Solving Pdes Using Laplace Transforms

Solving PDEs using Laplace Transforms, Chapter 15 Given a function  $u(x;t)$  defined for all  $t > 0$  and assumed to be bounded we can apply the Laplace transform in  $t$  considering  $x$  as a parameter.  $L(u(x;t)) = \int_0^\infty e^{-st} u(x;t) dt = U(x;s)$  In applications to PDEs we need the following:  $L(u_t(x;t)) = \int_0^\infty e^{-st} u_t(x;t) dt = e^{-st} u(x;t) \Big|_0^\infty + s \int_0^\infty e^{-st} u(x;t) dt = -sU(x;s) + u(x;0)$  so we have  $L(u_t(x;t)) = -sU(x;s) + u(x;0)$

Solving PDEs using Laplace Transforms, Chapter 15

Given a PDE in two independent variables  $x$  and  $t$ , we use the Laplace transform on one of the variables (taking the transform of everything in sight), and derivatives in that variable become multiplications by the transformed variable  $s$ . The PDE

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becomes an ODE, which we solve.

### DIFFYQS Solving PDEs with the Laplace transform

Laplace transforms can be used solve linear PDEs. Laplace transforms applied to the t variable (change to s) and the PDE simplifies to an ODE in the x variable. Recall the Laplace transform for  $f(t)$ .  $L\{f(t)\} = \int_0^\infty e^{-st} f(t) dt = F(s)$ ;  $L^{-1}\{F(s)\} = f(t)$  Apply the Laplace transform to  $u(x;t)$  and to the PDE.  $L\{u(x;t)\} = U(x;s)$ ;  $L^{-1}\{U(x;s)\} = u(x;t)$  The Laplace transform changes the derivatives with respect to t but NOT x:  $L\{u_t\} = sU - u(x;0)$

### Laplace Transforms to Solve BVPs for PDEs

$U(x, s) = C_1 \exp(-kx) + C_2 \exp(kx)$  By taking the Laplace transform of the two boundary conditions, I get the following:  $U(0, s) = u_0/s$ .  $U(L, s) = 0$ . Using the second boundary condition, I can calculate that  $C_2 = 0$ , and that the PDE in terms of x and s is:

### Using Laplace Transforms to solve a PDE

Using the Laplace transform on the equation gives, using the initial conditions, the equation:  $d^4 y/dx^4 + s^2 b^2 y = 0$ . The solution to this is:  $y(x, s) = A \cos(sbx) + B \cosh(sbx) + C \sin(sbx) + D \sinh(sbx)$

### Using Laplace transform on a partial differential equation ...

Applying the Laplace transform to (3) yields an inhomogeneous ODE in x. Solving this ODE using standard, but slightly involved, calculation, and then using the inversion formula in (6), we eventually obtain the expression for the solution  $u(x;t) = \frac{1}{4} \int_0^t u(x;0) dt$

### Transform Methods for Linear PDEs

1. Solution of ODEs using Laplace Transforms. Process Dynamics and Control. 2. Linear ODEs. For linear ODEs, we can solve without integrating by using Laplace transforms. Integrate out time and transform to Laplace domain Multiplication Integration. 3. Common Transforms.

### Solution of ODEs using Laplace Transforms

Example 1 1. Solve the differential equation given initial conditions. 2. Take the Laplace transform of both sides. Using the properties of the Laplace transform, we can transform this... 3. Solve for  $Y(s)$ . Simplify and factor the denominator to prepare for partial ...

### How to Solve Differential Equations Using Laplace Transforms

$u(x,t)e^{-ikx} dx = \lim_{h \rightarrow 0} \frac{1}{h} [u(x,t+h) - u(x,t)] = -tu_x(x,t)$  (3) To get two t-derivatives, we just apply this twice (with u replaced by  $u_t$  the first time)  $\int -2u_{tt}(x,t)e^{-ikx} dx = -t \int -tu_x(x,t)e^{-ikx} dx = -t^2 u_{xt}(x,t)$  So applying the Fourier transform to both sides of (1) gives. 2.

### Using the Fourier Transform to Solve PDEs

Laplace equation in half-plane. II. Replace Dirichlet boundary condition by Robin boundary condition  $u = u_{xx} + u_{yy} = 0, y > 0, -\infty < x < \infty, (u_y - \alpha u) |_{y=0} = h(x)$ . Then (16) should be replaced by  $(u_y - \alpha u) |_{y=0} = h(x)$ . and then  $A(\alpha) = -(\frac{1}{2} + \alpha) - 1 \cdot h(\alpha)$  and  $\hat{u}(x, y) = -\hat{h}(\alpha) (\frac{1}{2} + \alpha)$

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Applications of Fourier transform to PDEs

Question: Transform Methods 1. Solve The Following PDE Using Laplace Transforms  
 $u_x + u_y = 0$ ,  $u(0,t) = 0$ ,  $u(x,0) = 0$  Note That  $C[1] \Rightarrow 2$ . Solve With Laplace Transforms (Section 5.2 Kreyszig)  $Y'' - 4Y = 0$ ,  $Y(0) = 8$ ,  $Y'(0) = 7$

Solved: Transform Methods 1. Solve The Following PDE Using ...

In this video, I introduce the concept of Laplace Transforms to PDEs. A Laplace Transform is a special integral transform, and when it's applied to a differe...

Laplace Transforms for Partial Differential Equations (PDEs)

Applications of the Laplace transform in solving partial differential equations. Laplace transform of partial derivatives. Theorem 1. Given the function  $U(x, t)$  defined for  $a < x < b$ ,  $t > 0$ .

Laplace transform of partial derivatives. Applications of ...

We will tackle this problem using the Laplace Transform; but first, we try a simpler example \*\* just in this part of the notes, we use  $w(x,t)$  for the PDE, rather than  $u(x,t)$  because  $u(t)$  is conventionally associated with the step function A recap on the LT  $w'(t) + aw(t) = u(t)$ ,  $w(0) = 1$  We first solve the first order ODE

Can we do the same for PDEs? Is it ever useful?

First order PDEs  $a \frac{\partial u}{\partial x} + b \frac{\partial u}{\partial y} = c$ : Linear equations: change coordinate using  $(\tilde{x}; \tilde{y})$ , defined by the characteristic equation  $\frac{dy}{dx} = \frac{b}{a}$ ; and  $\tilde{y}(\tilde{x}; y)$  independent (usually  $\tilde{y} = x$ ) to transform the PDE into an ODE. Quasilinear equations: change coordinate using the solutions of  $\frac{dx}{ds} = a$ ;  $\frac{dy}{ds} = b$  and  $\frac{du}{ds} = c$  to get an implicit form of the solution  $\tilde{u}(\tilde{x}; \tilde{y}; u) = F(\tilde{x}; \tilde{y}; u)$ .

Analytic Solutions of Partial Differential Equations

INTRODUCTION The Laplace transform can be helpful in solving ordinary and partial differential equations because it can replace an ODE with an algebraic equation or replace a PDE with an ODE. Another reason that the Laplace transform is useful is that it can help deal with the boundary conditions of a PDE on an infinite domain.

PARTIAL DIFFERENTIAL EQUATIONS

This PDE may seem simple and even a bit pointless to analyse, but surprisingly a lot of analysis of PDEs in general can be done using solutions of Laplace's equation.

PDEs using Fourier Analysis II. In my previous post, PDEs ...

Transform methods provide a bridge between the commonly used method of separation of variables and numerical techniques for solving linear partial differential equations. While in some ways similar to separation of variables, transform methods can be effective for a wider class of problems.

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